

$$8\cos^4 x = 11\cos 2x - 1$$

$$8\left[\frac{1+\cos 2x}{2}\right]^2 = 11\cos 2x - 1$$

$$8 \cdot \frac{1+2\cos 2x + \cos^2 2x}{4} - 11\cos 2x + 1 = 0$$

$$2 + 4\cos 2x + 2\cos^2 2x - 11\cos 2x + 1 = 0$$

$$3 - 7\cos 2x + 2\cos^2 2x = 0$$

$$\cos 2x = t$$

$$2t^2 - 7t + 3 = 0$$

$$D = 49 - 26 = 5^2$$

$$t = \frac{7+5}{4} = 3$$

$$t = \frac{2}{4} = \frac{1}{2}$$

$\cos 2x = 3$  - не имеет смысла

$$\cos 2x = \frac{1}{2}$$

$$2x = \pm \frac{\pi}{3} + 2\pi k$$

$$x = \pm \frac{\pi}{6} + \pi k$$

$$\sin^4 x + \cos^4 x = \sin x \cos x$$

$$\sin^4 x + 2(\sin^2 x \cdot \cos^2 x) + \cos^4 x - 2(\sin^2 x \cdot \cos^2 x) = \sin x \cos x$$

$$(\sin^2 x + \cos^2 x)^2 - 2(\sin^2 x \cdot \cos^2 x) = \sin x \cos x$$

$$1 - 2(\sin^2 x \cdot \cos^2 x) = \sin x \cos x$$

$$\sin x \cos x = t$$

$$2t^2 + t - 1 = 0$$

$$D = 1 + 8 = 9$$

$$t = \frac{-1+3}{4} = \frac{1}{2}$$

$$t = -1 \quad \sin x \cos x = -1 \quad \text{НЕВОЗМОЖНО}$$

$$\sin x \cos x = \frac{1}{2}$$

$$2\sin x \cos x = 1$$

$$\sin 2x = 1$$

$$2x = \frac{\pi}{2} + 2\pi k$$

$$x = \frac{\pi}{4} + \pi k$$

$$\text{Otvet: } x = \frac{\pi}{4} + \pi k$$